

# Implementation of algorithms and data structures

## 2. seminar

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**Winter semestr 2025/26**

Last change 16. října 2025

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## AVL tree

Binary search tree where for every vertex, the difference between heights of the left and the right subtree is at most one.

## Write tests verifying consistency of AVL tree

- There is a template on gitlab
- Implement one function testing consistency of AVL tree
- Some unit tests are given, but there are more of them on recodex

## Motivation

- We need to test some parts of codes which are rarely executed
  - E.g.: Some cases in red-black trees
- It is hard to create tested configuration using API
  - E.g.: How to find a sequence of operations Insert/Delete for every case in red-black trees?
- Fuzz tests may create tested configuration, but data are too large for easy debugging

# Manually created data in memory: Basic idea

```
1 class Node:
2     def __init__(self, key, left, right, parent, is_black, size):
3         self.key = key
4         self.left = left
5         self.right = right
6         self.parent = parent
7         self.is_black = is_black
8         self.size = size
9
10 def test_delete_case_uncle_is_black():
11     root = Node(10, None, None, None, True, 6)
12     p = root.left = Node(5, None, None, root, False, 4)
13     l = p.left = Node(2, None, None, p, True, 2)
14     u = root.right = Node(15, None, None, root, True, 1)
15     ...
16     integrity_test(root)
17     root.delete(2)
18     integrity_test(root)
19     TEST(root.left == u)
20     TEST(u.is_black == False)
21     ...
```

## Discussion

- Simple approach to create one small test
- Impractical to create a larger test or multiple tests
  - Setting every variable is time-consuming,
  - hard to read, and
  - leads to unintentional bugs.

## Approach

- Encode data into compact and clear format, e.g.
  - XML, JSON
  - Custom format, e.g. (3,(1,(0,(,)),(2,(,))), (4,(,)))  
`https://gitlab.kam.mff.cuni.cz/datovsky/assignments/-/blob/e9a90994c0373599d5140341c567780f226cbf04/02-splay\_operation/cpp/splay\_tests.txt`
  - Use syntax of used programming language
- Write a function reading the chosen format

## Encode data: example

```
1 def subtree(key, is_black, left=None, right=None):
2     node = Node()
3     node.key = key
4     node.is_black = is_black
5     node.left = left
6     node.right = right
7     node.size = 1 + (left.size if left else 0) +
8                   (right.size if right else 0)
9     if left:
10        left.parent = self
11    if right:
12        right.parent = self
13    return node
14
15 root =
16     subtree(5, True,
17         subtree(3, False,
18             None,
19             subtree(4, True)),
20         subtree(7, True))
```

## Goal

Test that the resulting tree after an operation is as expected.

## Motivation

Testing every single variable of every node is really tedious, e.g.

```
1 TEST(root.key == 10)
2 TEST(root.left.is_black == False)
3 TEST(root.right.left.left.right.left == None)
4 ...
```

## Approach

- Encode input and expected output trees
- Decode both trees
- Turn tested operation on decoded input
- Compare result and the decoded expected result

## Compare obtained and expected results

```
1 def compare_trees(tested_tree, expected_tree):
2
3     def recursive(tested_node, expected_node):
4         TEST(tested_node.key == expected_node.key)
5         TEST(tested_node.is_black == expected_node.is_black)
6         if expected_node.left:
7             TEST(tested_node.left)
8             recursive(tested_node.left, expected_node.left)
9         else:
10            TEST(not tested_node.left)
11    ...
12
13    recursive(tested_tree.root, expected_tree.root)
```

```
1 tested_tree = Tree(...)
2 tested_tree.integrity_tests()
3 tested_tree.insert(5)
4 tested_tree.integrity_tests()
5 expected_tree = Tree(...)
6 expected_tree.integrity_tests()
7 compare_trees(tested_tree, expected_tree)
```

- It is hard to see what is stored in memory
- Without the knowledge of stored data debugging is difficult
- Visualize stored data!
- Content of an array can be easily printed on terminal
- Advanced structures needs graphical presentation

# Write the structure of a red-black tree

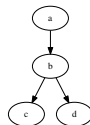
```
1 void rb_print(rb_tree *tree) {
2     rb_print(tree, tree->root);
3     printf("\n");
4 }
5
6 void rb_print(rb_tree *tree, rb_node *node) {
7     if(!node)
8         printf("L");
9     else {
10        printf("(");
11        rb_print(tree, node->left);
12        printf("%d", node->key);
13        if(node->is_red())
14            printf("R");
15        rb_print(tree, node->right);
16        printf(")");
17    }
18 }
```

## Output

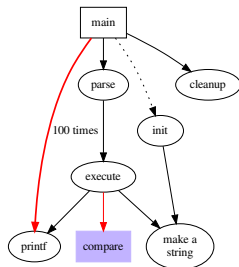
- (((L1L)2(L3L))4(((L6RL)7L)10((L14RL)20L)))
- Output can be improved using ASCII-art
- Graphic visualization may be clearer

# Examples of graphs created in DOT

```
1 digraph graphname {
2   a -> b -> c;
3   b -> d;
4 }
```



```
1 digraph G {
2   size = "4,4";
3   main [shape=box]; /* this is a comment */
4   main -> parse [weight = 8];
5   parse -> execute;
6   main -> init [style=dotted];
7   main -> cleanup;
8   execute -> {make_string printf}
9   init -> make_string;
10  edge [color=red]; // so is this
11  main -> printf [style=bold,label="100 times"];
12  make_string [label="make a\nstring"];
13  node [shape=box,style=filled,color=".7 .3 1.0"];
14  edge [color=red];
15  execute -> compare;
16 }
```



More examples: <https://graphviz.org/gallery/>

# Write the structure of a red-black tree using DOT

```
1 void rb_print(rb_tree *tree) {
2     print("digraph G {\n")
3     rb_print(tree, tree->root);
4     printf("}\n");
5 }
6
7 void rb_print(rb_tree *tree, rb_node *node) {
8     if(node) {
9         printf("%s [color=%s];\n", node->key, node->is_red ? "red" :
10             "black");
11         if(node->parent)
12             printf("%s -> %s;\n", node->parent->key, node->key);
13         rb_print(tree, node->left);
14         rb_print(tree, node->right);
15     }
```

# Create a graphviz picture in Python

```
1 import pydot
2
3 graph = pydot.Dot("my_graph", graph_type="graph", bgcolor="yellow")
4
5 # Add nodes
6 my_node = pydot.Node("a", label="Foo")
7 graph.add_node(my_node)
8 # Or, without using an intermediate variable:
9 graph.add_node(pydot.Node("b", shape="circle"))
10
11 # Add edges
12 my_edge = pydot.Edge("a", "b", color="blue")
13 graph.add_edge(my_edge)
14 # Or, without using an intermediate variable:
15 graph.add_edge(pydot.Edge("b", "c", color="blue"))
16
17 # Output image in png format
18 graph.write_png("output.png")
19
20 # Convert to string
21 output_raw_dot = graph.to_string()
22 # Or, save it as a DOT-file:
23 graph.write_raw("output_raw.dot")
```

## Language bindings (API)

- Python
- Java
- Matlab
- Wordpress
- LaTeX: Tikz, dot2tex: A Graphviz to LaTeX converter

## Visualization and IDE integrations

- Graphviz (dot) language support for Visual Studio Code
- Graphviz Visual Editor: A web application
- Qt Visual Graph Editor (C++)
- More resources about graphviz

## Other graph visualization tools

- NetworkX
- Gephi
- igraph