# NTIN090 — Introduction to complexity and computability theory

Exam questions, academic year 2019/20 Petr Kučera

Two questions will be asked during the oral part of the exam according to one of the following two schemes:

- One question of group A and one question of group D.
- One question of group B and one question of group C.

## Α

- (A1) Rice's theorem.
- (A2) Post correspondence problem.
- (A3) Savitch's theorem.
- (A4) Deterministic space hierarchy.
- (A5) Deterministic time hierarchy.
- (A6) NP-completeness of TILING.
- (A7) Fully polynomial time approximation scheme for the KNAPSACK problem.

#### В

- (B1) Gödel number, universal Turing machine, undecidability of the language of universal Turing machine (acceptance) and Halting problem.
- (B2) RAM and its equivalence with Turing machines.
- (B3) Enumerators of partially decidable and decidable languages.
- (B4) Polynomial reduction of TILING to SATISFIABILITY.
- (B5) Polynomial reduction of Satisfiability to 3-Satisfiability.
- (B6) Polynomial reduction of 3-Dimensional Matching to Partition.
- (B7) Pseudopolynomial algorithm for the KNAPSACK problem. Pseudopolynomial algorithms and strong NP-completeness (definitions).

# С

- (C1) Definition of *m*-reducibility and completeness, *m*-completeness of the language of a universal Turing machine, the Halting problem and their diagonals (languages  $L_u$ , HALT, DIAG, and HALT-DIAG).
- (C2) Basic complexity classes and their relations.
- (C3) Approximation algorithms, example (BIN PACKING).

## D

- (D1) (Turing) decidable and partially decidable languages and their basic properties (closedness properties, Post's theorem).
- (D2) The (two) definitions of class NP and their equivalence.
- (D3) Inapproximability of Travelling Salesperson.
- (D4) Pseudopolynomial algorithms and strong NP-completeness (definitions). Strong NP-completeness of Travelling Salesperson.
- (D5) Approximation schemes (definition), connection to strong NP-completeness.
- (D6) Class co-NP and co-NP-completeness.